

Looking into possible conversions of PM into AM due to off-optimal setting of the SB frequencies. When we look into the power transmission of a cavity:

$$I_{\text{transmitted}} = I_0 \frac{1}{1 + F * \sin^2(\frac{\delta}{2})} \quad (1)$$

with

$$\delta = 2\pi \frac{\Delta s}{\lambda} + \Delta\phi \quad (2)$$

We can then express off-optimal SB frequencies ( $\Delta f \neq 0$ ) in terms of  $\Delta\phi$ : The phase that the off-optimal SB accumulates with regard to the optimal SB.

$$\Delta\phi = \frac{\omega}{c} L = \frac{2\pi(1 \text{ kHz})}{3E8 \frac{\text{m}}{\text{s}}} 21.2 \text{ m} = 4.44E - 4 \text{ rad} \quad (3)$$

$$\Rightarrow \frac{\delta}{2} = 2.2201E - 4 \text{ rad} \quad (4)$$

For a finesse  $F = 1548$  this leads to

$$\Delta I_{\text{transmitted}} = 1 - \frac{1}{1 + 1548 \sin^2(2.2201E - 4)} = 7.63E - 5 \frac{\Delta f}{1 \text{ kHz}} \quad (5)$$

Now all the power here is from the 11 MHz SB ( $m_{\text{PM}} = 0.17$ )  $\Rightarrow m_{\text{AM}} = 0.17 * 7.65E - 5 = 1.30E - 5$ . Also we learn

$$\frac{m_{\text{PM}_{11 \text{ MHz}}}}{m_{\text{AM}_{11 \text{ MHz}}}} = \frac{0.17}{7.63E - 5} = 2228 \frac{1 \text{ kHz}}{\Delta f} \quad (6)$$

The 55 MHz SB is generated by multiplying the 11 MHz SB by 5. So the accumulated phase  $\Delta\phi$  and therefore  $\delta/2$  are also multiplied by 5. This leads to

$$\frac{m_{\text{PM}_{55 \text{ MHz}}}}{m_{\text{AM}_{55 \text{ MHz}}}} = \frac{0.19}{0.001904} = 99.80 \frac{1 \text{ kHz}}{\Delta f} \quad (7)$$